

## AS Level Further Mathematics A

### Y533 Mechanics

#### Sample Question Paper

Version 2

## Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes

#### You must have:

- Printed Answer Booklet
- Formulae AS Level Further Mathematics A

#### You may use:

- a scientific or graphical calculator



### INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question.
- The acceleration due to gravity is denoted by  $g \text{ m s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use  $g = 9.8$ .

### INFORMATION

- The total number of marks for this paper is **60**.
- The marks for each question are shown in brackets [ ].
- **You are reminded of the need for clear presentation in your answers.**
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **8** pages.

2

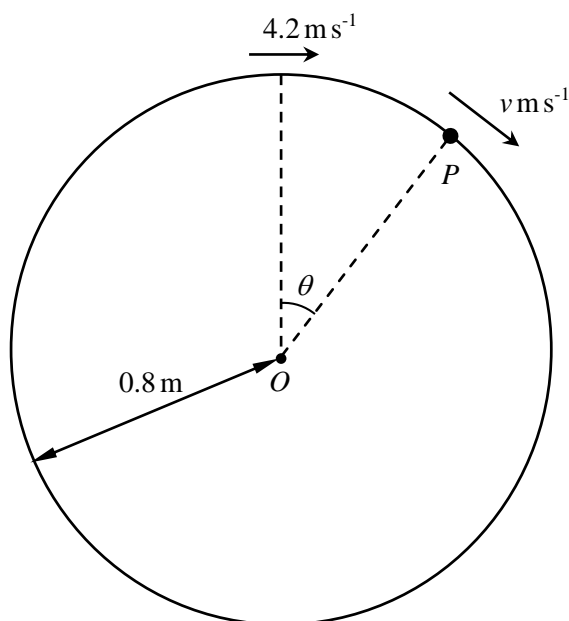
Answer **all** the questions.

1 A roundabout in a playground can be modeled as a horizontal circular platform with centre  $O$ . The roundabout is free to rotate about a vertical axis through  $O$ . A child sits without slipping on the roundabout at a horizontal distance of 1.5 m from  $O$  and completes one revolution in 2.4 seconds.

(i) Calculate the speed of the child. [3]

(ii) Find the magnitude and direction of the acceleration of the child. [3]

2



A smooth wire is shaped into a circle of centre  $O$  and radius  $0.8\text{ m}$ . The wire is fixed in a vertical plane. A small bead  $P$  of mass  $0.03\text{ kg}$  is threaded on the wire and is projected along the wire from the highest point with a speed of  $4.2\text{ m s}^{-1}$ . When  $OP$  makes an angle  $\theta$  with the upward vertical the speed of  $P$  is  $v\text{ m s}^{-1}$  (see diagram).

(i) Show that  $v^2 = 33.32 - 15.68\cos\theta$ . [4]

(ii) Prove that the bead is never at rest. [1]

(iii) Find the maximum value of  $v$ . [2]

- 3 (i) Write down the dimension of density. [1]

The workings of an oil pump consist of a right, solid cylinder which is partially submerged in oil. The cylinder is free to oscillate along its central axis which is vertical. If the base area of the pump is  $0.4 \text{ m}^2$  and the density of the oil is  $920 \text{ kg m}^{-3}$  then the period of oscillation of the pump is  $0.7 \text{ s}$ .

A student assumes that the period of oscillation of the pump is dependent only on the density of the oil,  $\rho$ , the acceleration due to gravity,  $g$ , and the surface area,  $A$ , of the circular base of the pump. The student attempts to test this assumption by stating that the period of oscillation,  $T$ , is given by  $T = C\rho^\alpha g^\beta A^\gamma$  where  $C$  is a dimensionless constant.

- (ii) Use dimensional analysis to find the values of  $\alpha$ ,  $\beta$  and  $\gamma$ . [4]

- (iii) Hence give the value of  $C$  to 3 significant figures. [2]

- (iv) Comment, with justification, on the assumption made by the student that the formula for the period of oscillation of the pump was dependent on only  $\rho$ ,  $g$  and  $A$ . [2]

- 4 A car of mass  $1250 \text{ kg}$  experiences a resistance to its motion of magnitude  $kv^2 \text{ N}$ , where  $k$  is a constant and  $v \text{ m s}^{-1}$  is the car's speed. The car travels in a straight line along a horizontal road with its engine working at a constant rate of  $P \text{ W}$ . At a point  $A$  on the road the car's speed is  $15 \text{ m s}^{-1}$  and it has an acceleration of magnitude  $0.54 \text{ m s}^{-2}$ . At a point  $B$  on the road the car's speed is  $20 \text{ m s}^{-1}$  and it has an acceleration of magnitude  $0.3 \text{ m s}^{-2}$ .

- (i) Find the values of  $k$  and  $P$ . [7]

The power is increased to  $15 \text{ kW}$ .

- (ii) Calculate the maximum steady speed of the car on a straight horizontal road. [3]

5



The masses of two spheres  $A$  and  $B$  are  $3m$  kg and  $m$  kg respectively. The spheres are moving towards each other with constant speeds  $2u$  m s<sup>-1</sup> and  $u$  m s<sup>-1</sup> respectively along the same straight line towards each other on a smooth horizontal surface (see diagram). The two spheres collide and the coefficient of restitution between the spheres is  $e$ . After colliding,  $A$  and  $B$  both move in the same direction with speeds  $v$  m s<sup>-1</sup> and  $w$  m s<sup>-1</sup>, respectively.

(i) Find an expression for  $v$  in terms of  $e$  and  $u$ . [6]

(ii) Write down unsimplified expressions in terms of  $e$  and  $u$  for

(a) the total kinetic energy of the spheres before the collision, [1]

(b) the total kinetic energy of the spheres after the collision. [2]

(iii) Given that the total kinetic energy of the spheres after the collision is  $\lambda$  times the total kinetic energy before the collision, show that

$$\lambda = \frac{27e^2 + 25}{52}.$$

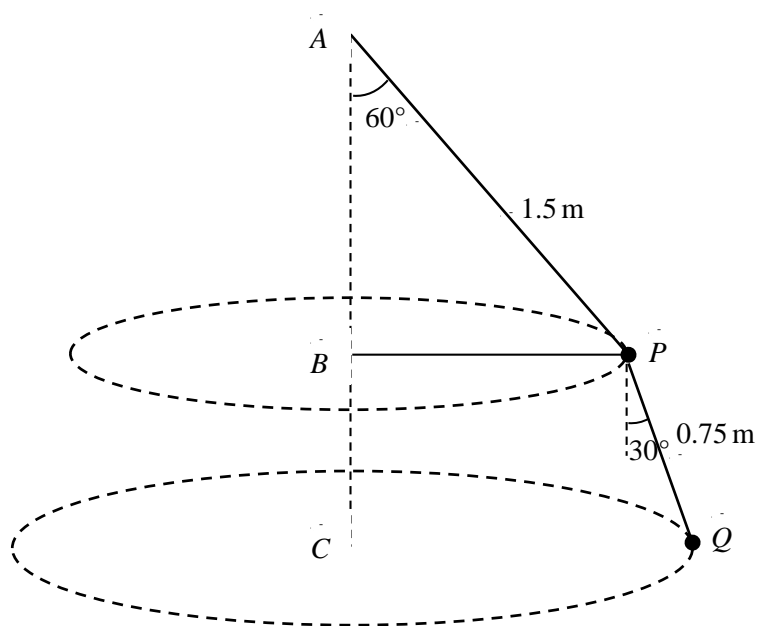
[3]

(iv) Comment on the cases when

(a)  $\lambda = 1$ ,

(b)  $\lambda = \frac{25}{52}$ .

[3]



The fixed points  $A$ ,  $B$  and  $C$  are in a vertical line with  $A$  above  $B$  and  $B$  above  $C$ . A particle  $P$  of mass  $2.5$  kg is joined to  $A$ , to  $B$  and to a particle  $Q$  of mass  $2$  kg, by three light rods where the length of rod  $AP$  is  $1.5$  m and the length of rod  $PQ$  is  $0.75$  m. Particle  $P$  moves in a horizontal circle with centre  $B$ . Particle  $Q$  moves in a horizontal circle with centre  $C$  at the same constant angular speed  $\omega$  as  $P$ , in such a way that  $A$ ,  $B$ ,  $P$  and  $Q$  are coplanar. The rod  $AP$  makes an angle of  $60^\circ$  with the downward vertical, rod  $PQ$  makes an angle of  $30^\circ$  with the downward vertical and rod  $BP$  is horizontal (see diagram).

- (i) Find the tension in the rod  $PQ$ . [2]
- (ii) Find  $\omega$ . [3]
- (iii) Find the speed of  $P$ . [1]
- (iv) Find the tension in the rod  $AP$ . [3]
- (v) Hence find the magnitude of the force in rod  $BP$ .  
Decide whether this rod is under tension or compression. [4]

**END OF QUESTION PAPER**

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